

# Market-Beta

Ivo Welch

May 2019

# Notice to PhD Students

This presentation is intended to teach how not to commit suicide on the job market.

# Notice to PhD Students

This presentation is intended to teach how ~~not~~ to commit suicide on the job market.

# Because, what you need is



I am not saying it's right.  
I am saying I am impressed.

(PS: On the job market, it will be cleverness, not necessarily mathiness, that matters.)

# Why Not Job Market?

- ▶ My brownbag paper is way too simple,
- ▶ ...and it is not about
  - ▶ new data,
  - ▶ big data,
  - ▶ new small data,
  - ▶ and/or clever quasi-experimental identification.

# Why Not Job Market?

- ▶ My brownbag paper is way too simple,
- ▶ ...and it is not about
  - ▶ new data,
  - ▶ big data,
  - ▶ new small data,
  - ▶ and/or clever quasi-experimental identification.

# So why bother?

- ▶ It's actually very useful, and
- ▶ you will actually want to use this in your lifetime,
- ▶ ...and it saved your Wednesday lunch.

2				
3	<b>Date</b>	<b>Name</b>		
4	Wednesday, April 10, 2019			
5	Wednesday, April 17, 2019			
6	Wednesday, April 24, 2019			only if no one else wants to present: Ivo Welch
7	Wednesday, May 1, 2019	Bernard Herskovic		
8	Wednesday, May 8, 2019			



- ▶ so no complaints, please.

# So why bother?

- ▶ It's actually very useful, and
- ▶ you will actually want to use this in your lifetime,
- ▶ ...and it saved your Wednesday lunch.

	<b>Date</b>	<b>Name</b>		
4	Wednesday, April 10, 2019			
5	Wednesday, April 17, 2019			
6	Wednesday, April 24, 2019			
7	Wednesday, May 1, 2019	Bernard Herskovic		
8	Wednesday, May 8, 2019			

only if no one else wants to present: Ivo Welch



- ▶ so no complaints, please.



# Breaks Chernov Rule

- ▶ not “serious” research
- ▶ instead: this is a “Tinker With Data” paper

# Breaks Chernov Rule

- ▶ not “serious” research
- ▶ instead: this is a “Tinker With Data” paper

# Motivation

Why still bother with “boring” old market-beta?

- ▶ Market-beta is interesting even w/o CAPM
  - ▶ Measure of risk contribution to diversified portfolios.
  - ▶ Hedging against bear markets
  - ▶ Down-Beta Theories (as in Ang+ or Lettau+)
  - ▶ Betting against Beta (as in Frazzini-Pedersen)
  - ▶ Pragmatic: used in regulation, etc.
- ▶ How should we estimate beta?
  - ▶ And can it make a difference?

# Performance Metric

I will judge beta quality by prediction.

- ▶ future ols(/other) 1-mo or 1-yr market-beta **estimates**
- ▶ never future average returns.
- ▶ PS: If two proxies are drawn with noise from true value, the expected  $R^2$  of each proxy with the true value is the squareroot of the  $R^2$  of one proxy with the other proxy.

# Performance Metric

I will judge beta quality by prediction.

- ▶ future ols(/other) 1-mo or 1-yr market-beta **estimates**
- ▶ never future average returns.
- ▶ PS: If two proxies are drawn with noise from true value, the expected  $R^2$  of each proxy with the true value is the squareroot of the  $R^2$  of one proxy with the other proxy.

# Best Beta Estimator Known: Vasicek

- ▶ random-effects estimator = bayesian shrinkage
- ▶ Run OLS Regressions
- ▶ Calculate x-sect means and sds of betas
- ▶ For each stock,

$$b_{VCK} = w \cdot b_{XS} + (1 - w) \cdot b_{TS},$$

where  $w = \sigma_{TS} / (\sigma_{TS} + \sigma_{XS})$ .

# Other Important Choices

- ▶ Always use daily stock returns
- ▶ about 1-3 years of data.
- ▶ Never use industry beta for individual stocks.
  - ▶ Indeed, less noisy;
  - ▶ but just like using “1” — low predictive power.
- ▶ vasicek and its derivatives
  - ▶ (random-effects and/or bayesian justification if no drift.)
  - ▶ Levi-Welch linear de-bias.

**more alternatives below: Dimson, Frazzini-Pedersen**

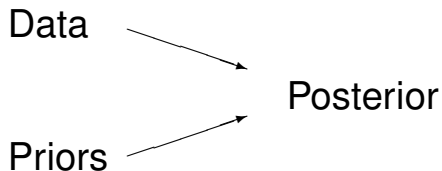
# Vasicek Disadvantages

- ▶ “Pseudo Optimal”
  - ▶ “optimal design” was never suited to problem:
  - ▶ vasicek is designed for measurement error,
  - ▶ not for underlying beta drift
  - ▶ (ergo 12–24 months windows)
- ▶ good  $R^2$ , but badly biased
  - ▶ levi-welch (2017) suggests empirical de-biasing
  - ▶ requires another stage
- ▶ spooky entangled estimates
- ▶ requires multi-step ts and xs procedure



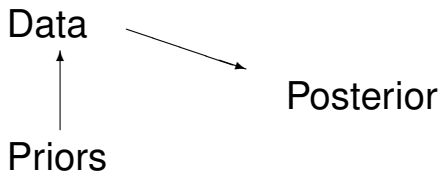
# Better and Simpler Estimator

# Standard Bayesian Use of Prior

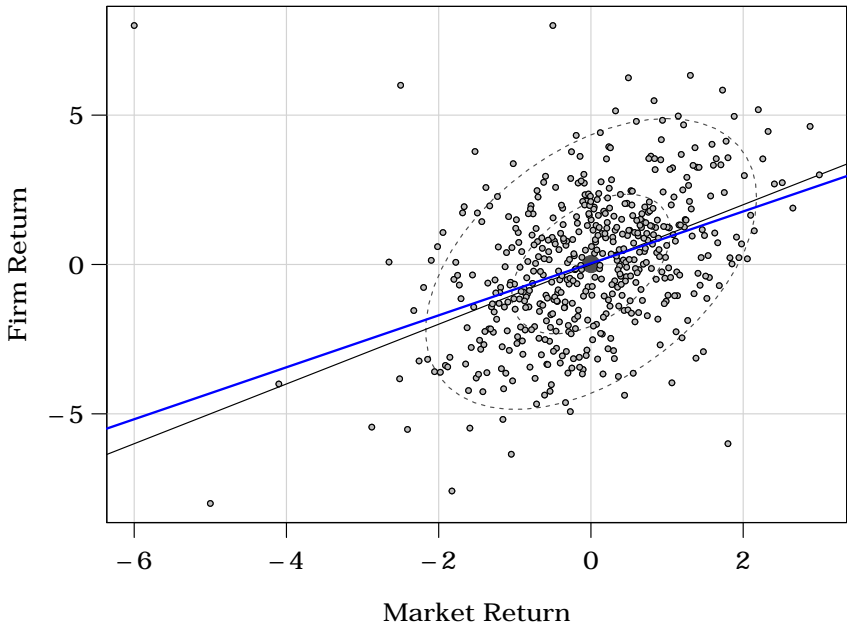


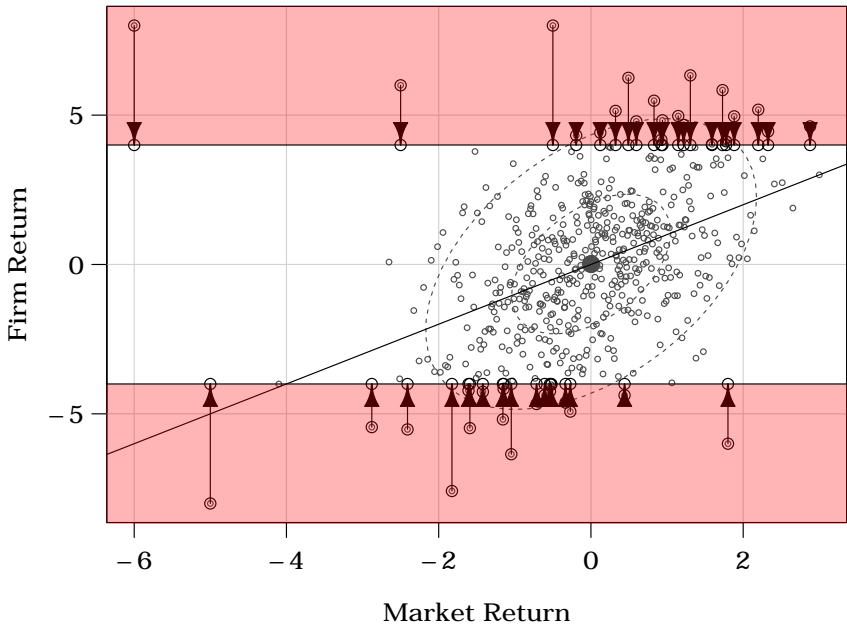
- ▶ Involves arguments about reasonable priors
- ▶ Often painful—days babysitting, not minutes.
- ▶ Usually primarily in dedicated papers

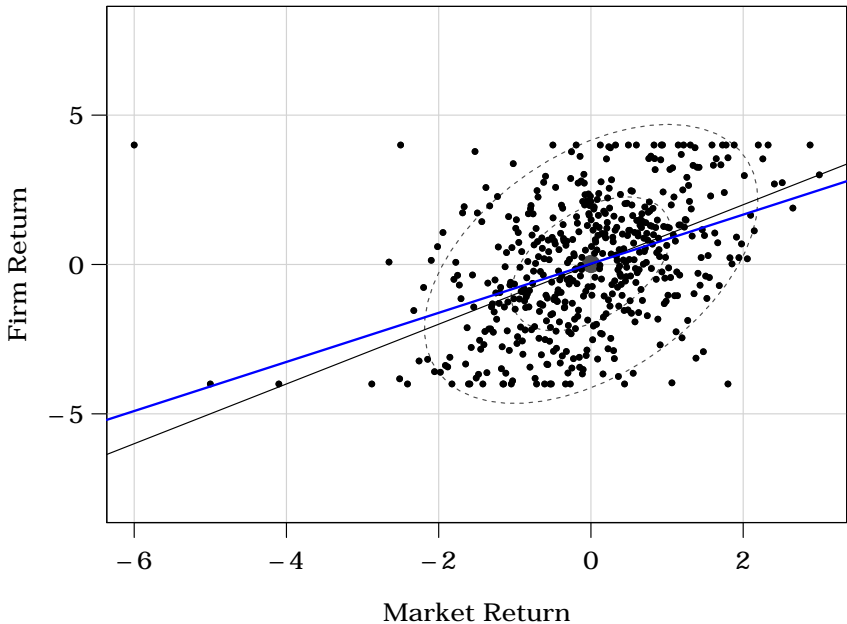
# (Ab-)Use of Prior

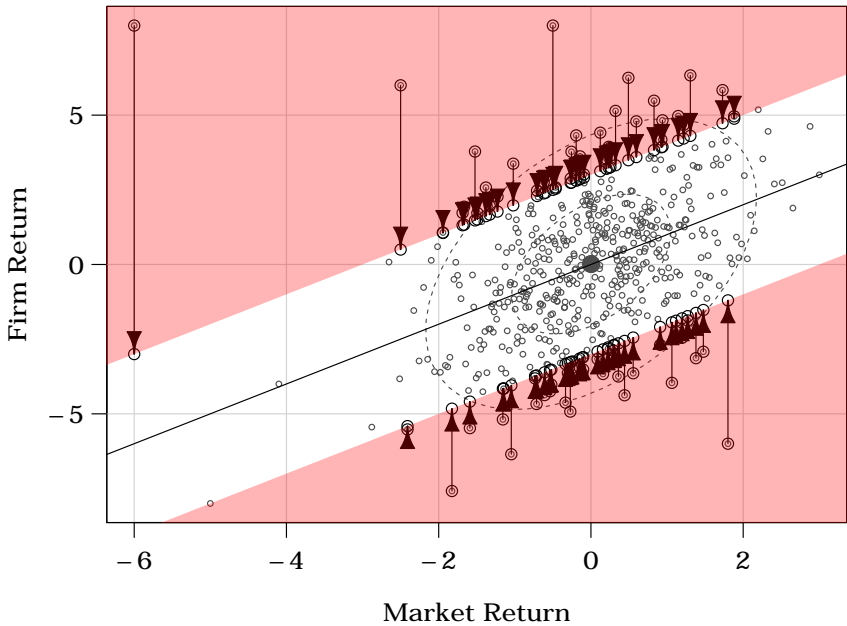


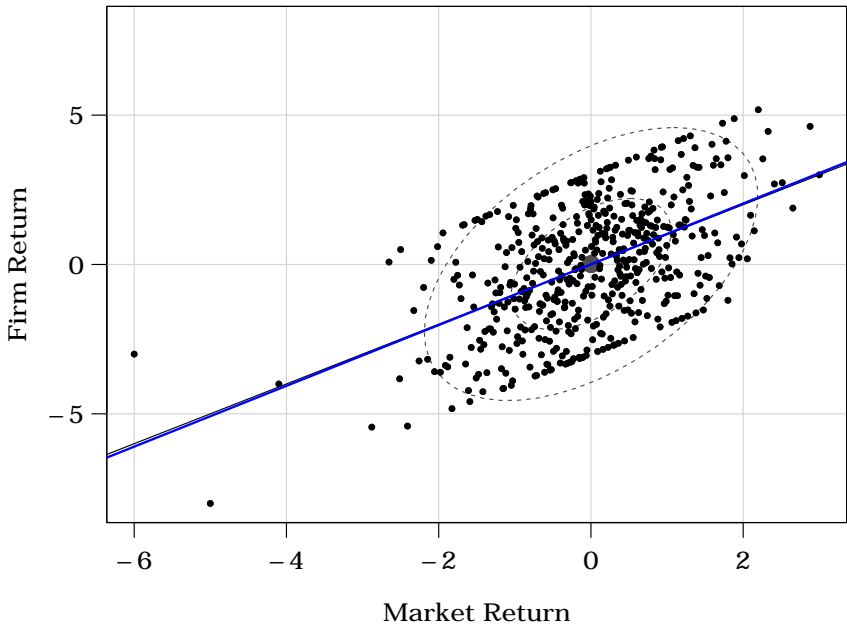
- ▶ Still involves arguments about reasonable priors
- ▶ Easy to use. minutes, not days.
- ▶ Likely novel method.



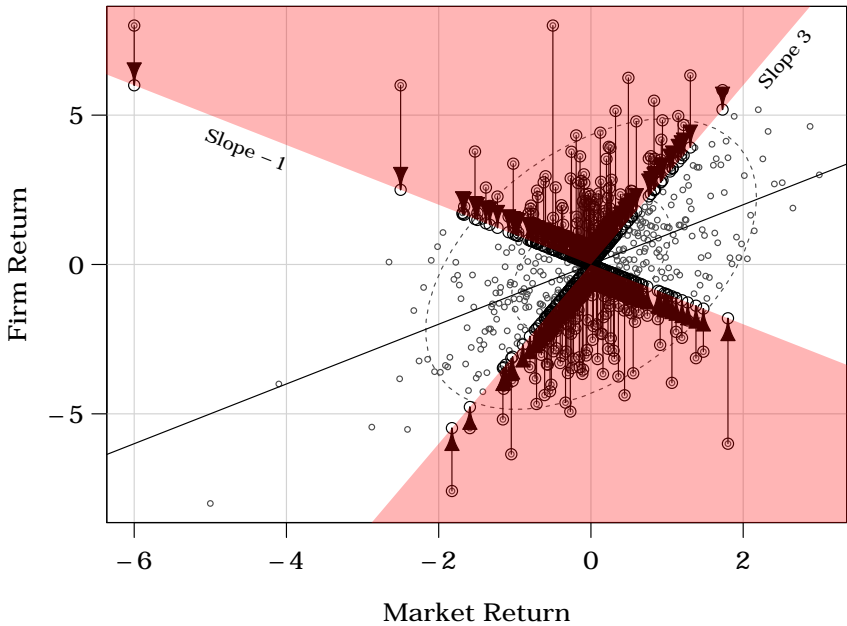


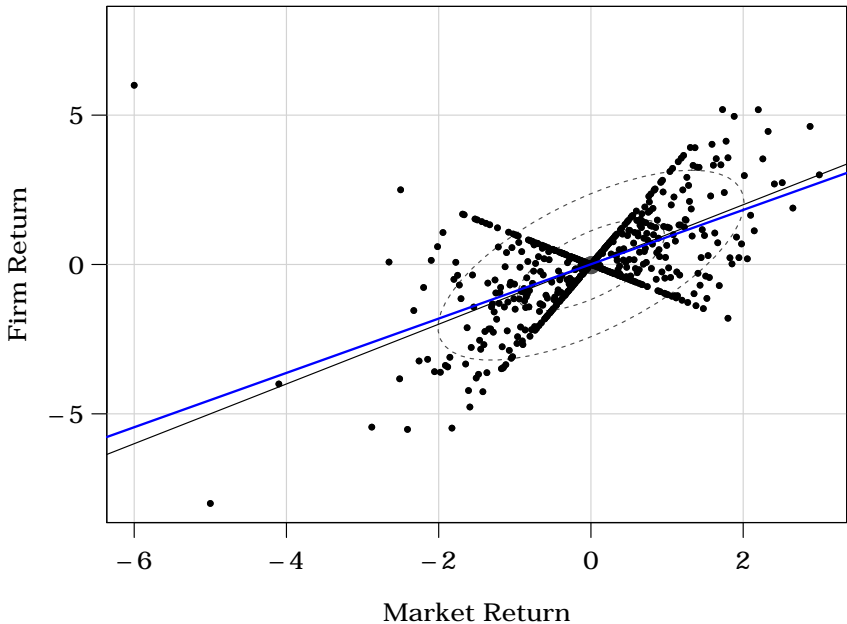












- ▶ non-Bayesian use of prior
- ▶ with wide priors, not very costly, even if panel is true OLS w/o outliers.
- ▶ Note: Even if  $\hat{b} = 0.8$ , the prior is still effective on individual points.
  - ▶ Bayesian OLS-type prior would work on overall  $\hat{b}$  estimate.
  - ▶ If final is near 1.0, Bayesian method says “just fine.”
  - ▶ Here, a prior(-1,3) still influences points, and thus even estimates close to 1.0. → can move a  $\hat{b}$  away from 1.0.
  - ▶ PS: could use Bayesian with priors on mixed distributions, plain + outliers. Would work, too, but far more painful.

# beta slope winsorized (bsw)

1. 12–24 mos of **daily** stock returns
2. winsorize all returns ( $\Delta_s = 2$ ):

$$rsw_{i,t} \in 1.0 + [-\Delta_s, \Delta_s] \cdot r_{m,t} \cdot$$

3. estimate ols market-model

$$rsw_{i,t} = a_i + bsw_i \cdot r_{m,t}$$

(just a reuse of the model with a reasonable prior. note: model-specific.)

# why $\Delta_S = 2$ ?

- ▶ fewer than 1% of betas exceed  $-1$  and  $+3$
- ▶ fewer than 0.03% repeat in consecutive years
  - ▶ (greater than  $1\% \cdot 1\%$ , but not by much.
- ▶ beyond, no monotonicity between  $b_t$  and  $E(b_{t+1})$
- ▶ not philosophical, but also not highly searched:
  - ▶ you could also use  $[-0.5, 2.5]$  or  $[-3, 5]$ .
  - ▶ lower  $\Delta_S$  forces too much towards 1.
  - ▶ higher  $\Delta_S$  forces nada.

# does it matter?

are betas even different?

$$\text{rmsd} ( \text{bols}_D , \text{bsw} ) \approx 0.37$$

$$\text{rmsd} ( \text{bvck}_D , \text{bsw} ) \approx 0.20$$

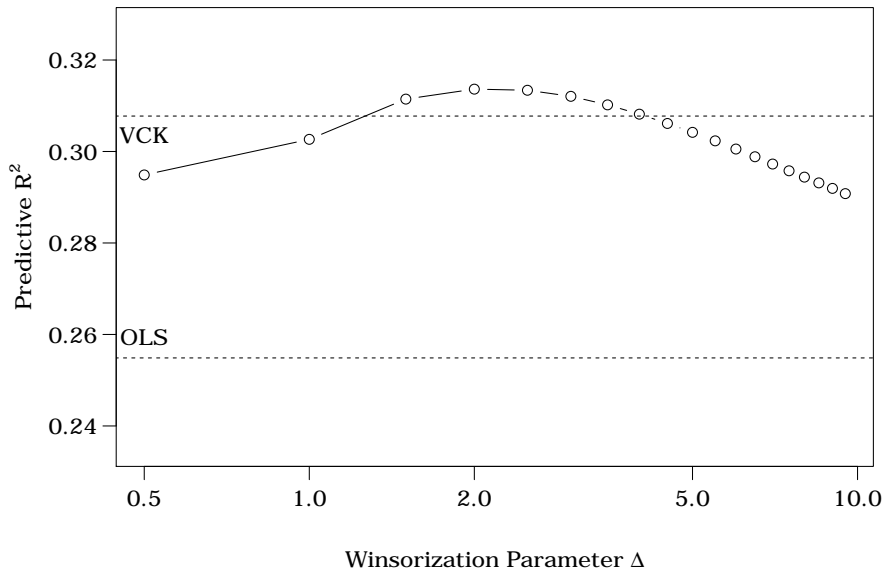
$$\text{rmsd} ( \text{bols}_M , \text{bsw} ) \approx 0.60$$

# “gamma” panel reg for bols<sub>t+1</sub>

Dependent: future 1-year **ols** beta from daily returns, same set.

	$\gamma_0$	se( $\gamma_0$ )	$\gamma_1$	se( $\gamma_1$ )	R <sup>2</sup>
(bols)	0.34	.004	0.54	.005	25.5%
(bvck)	0.19	.002	0.74	.002	30.8%
... (blw)	-0.01	.003	0.98	.003	same
level (blw)	0.27	.002	0.70	.003	29.7%
band (bbw)	0.04	.002	0.93	.003	30.9%
slope (bsw)	0.01	.002	0.96	.003	<b>31.4%</b>
slope + v	-0.01	.003	1.00	.003	31.5%

True R<sup>2</sup> is squareroot.  $\sqrt{.3} \approx 0.55$ .

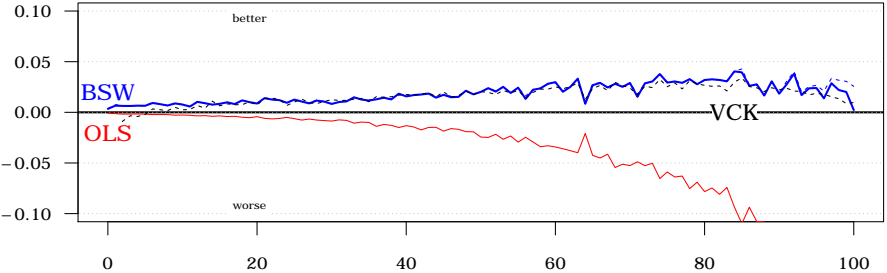
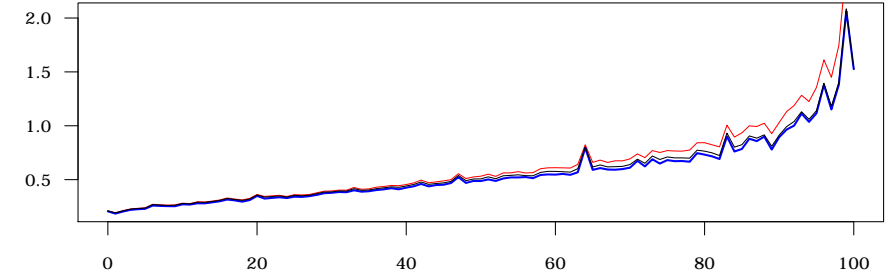




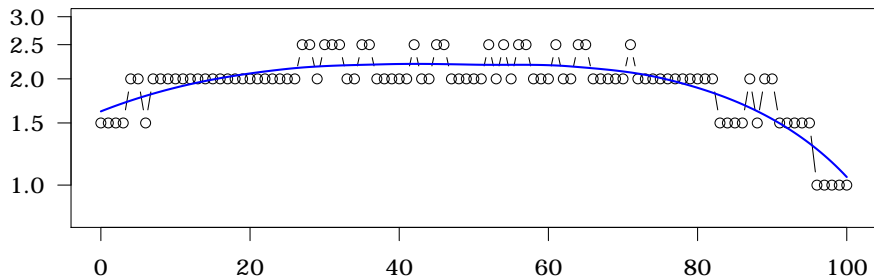
# Nothing Sensitive or Edgy

- ▶ very stable by year.
- ▶ very stable by ols beta.
- ▶ no meaningful improvement by varying  $\Delta_S$ .
  - ▶ even by own lagged beta, beta-sd, marketcap, trading volume, volatility, etc.

# RMSE by ols se(b) Percentile



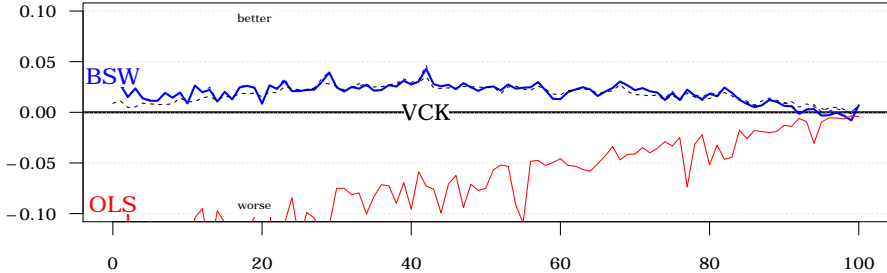
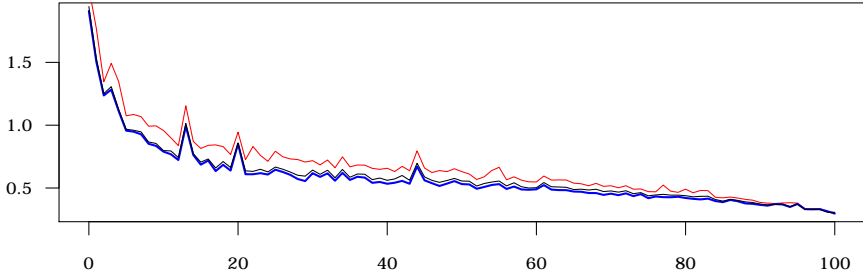
# $\Delta^*$ by ols se(b) Percentile



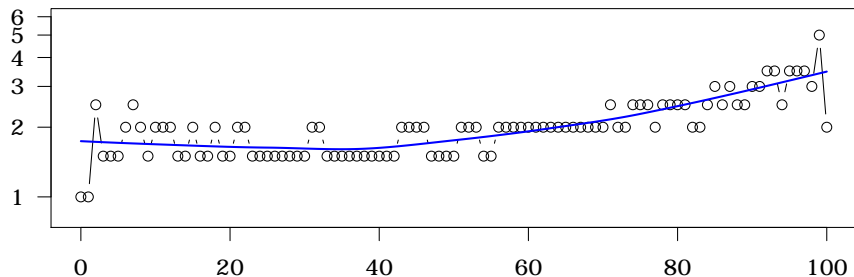
possible improvements: obtain ols b se rank, then

- ▶ more winsorization ( $\Delta_S = 1.5$ ) for  $> 85\%$  and 1 for  $> 95\%$ .
- ▶ but stable from 5 to 80 and look at absolute improvement,
- ▶ only the 95%+ do.
- ▶  $\Rightarrow$  1st-stage firm-specific deltas won't help much, on avg.

# RMSE by Market Cap Percentile



# $\Delta^*$ by market cap percentile



possible improvements: obtain mcap rank, then

- ▶ more winsorization ( $\Delta_S = 1.5$ ) for small-caps (rank < 40%),
- ▶ less winsorization ( $\Delta_S = 3$ ) for big-caps (rank > 80%).

# Another 2% $R^2$ Improvement

- ▶ retain 1-pass simplicity of use
- ▶ WLS market-model,  $w=f(\text{age})$

steep exponential decline:

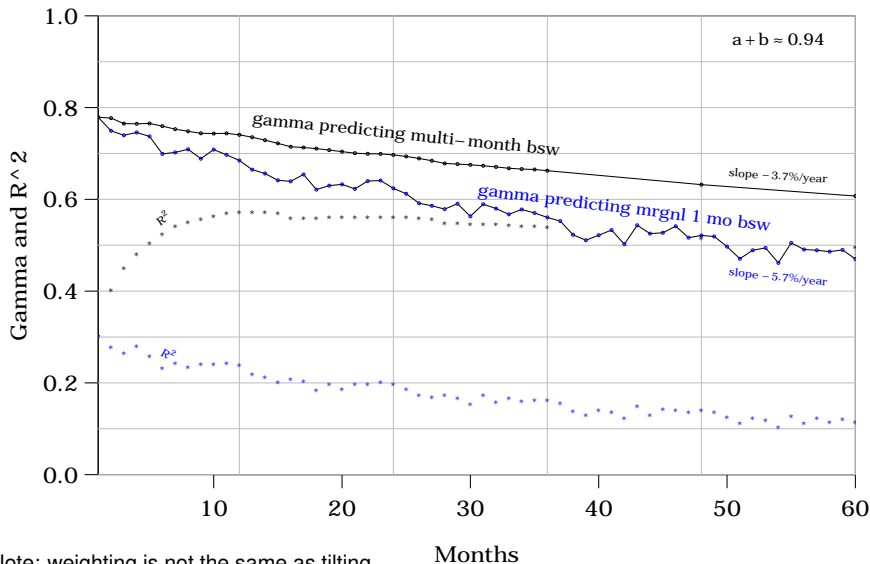
	Now	3 mo	6mo	1yr	2yr
WLS w	100%	80%	50%	10%	2%

- ▶ PS: this WLS decay allowed for a kink
- ▶ want approx formula?  $\approx \exp[-2(\Delta\text{days})/252]$
- ▶ trivially easy in time
- ▶ no marginal loss of observations

# PS: Mean Reversion on Monthly BSW

- ▶ not fixing outliers suggests faster mean reversion of beta
- ▶ need to estimate mean reversion of betas after fixing outliers

# PS: Mean Reversion on Monthly BSW



Note: weighting is not the same as tilting.

Note: dependent ne OLS, but BSW. Indep is WLS.BSW. Daily Stock Returns.



# another 1% $R^2$ improvement

- ▶ no longer simple, 1-pass, no-obs-loss
- ▶ add one extra variable reflecting firm-size or dollar trading volume.
  - ▶ big firms have bigger market-betas (yes!),
  - ▶ but use requires first-stage regression,
  - ▶ and marketcap requires merging, data loss, etc.
- ▶ I could find no other useful accounting compustat or crsp derived variable or ratio.

# Dimson + Frazzini-Pedersen

care for $y_{t+1} \downarrow$	<u><math>R^2</math> with <math>x_t</math> being only</u>				
	ols	bsw	vck	dim	fp
ols	38%	44%	43%	28%	27%

(Monthly-overlaps)

# Dimson + Frazzini-Pedersen

care for $y_{t+1} \downarrow$	$R^2$ with $x_t$ being only				
	ols	bsw	vck	dim	fp
ols	38%	44%	43%	28%	27%
vck		51%	50%		
bsw		57%			
dim		30%		22%	
fp		30%			21%

$\Rightarrow R^2$  to  $\beta_{\text{true}}$  should be  $\approx 75\%$

→ what should you use if you care (but why?) about future dimson or fp estimates?  
(Monthly-overlaps)

if you are interested in future Dimson beta,

→ use current bsw

never use current Dimson beta as estimator

if you are interested in future Frazzini-Pedersen beta.

→ use current bsw

never use current FP beta as estimator

did they ever try to validate their measures?

# Monthly-Frequency Return Data?

- ▶ even long-window monthly betas are miserable predictors of anything (like  $R^2$  of  $< 15\%$ , not  $40\%$ ).
- ▶ daily predicts monthly better than monthly itself.
- ▶ → use daily frequency even if interested in future monthly market betas.

# Future

Can some of this be generalized?

- ▶ To what extent can we use our prior information to manipulate the incoming data first,
- ▶ and then run plain classical procedures,
- ▶ because Bayesian methods are so painful that only dedicated B papers are using them.
- ▶ (e.g., stick fitted values  $w/ se$  [as weights?] from 1st-stage OLS into 2nd-stage OLS?)

# Conclusion

- ▶ novel slope winsorization method afaik, with use of prior in different way,
- ▶ novel application of winsorization method in important context of market-beta estimation.
- ▶ only simple use of prior. no 1st stage needed.
- ▶ superb ease of use. pto.

# So Why Not?

```
wins.rel <- function( r, rmin, rmax ) {  
  rl <- ifelse( (rmin<rmax), rmin, rmax )  
  ru <- ifelse( (rmin<rmax), rmax, rmin )  
  ifelse( r<rl, rl, ifelse(r>ru, ru, r) )  
}  
  
delta <- 2  
wri <- wins.rel( ri, (1-delta)*rm, (1+delta)*rm )  
  
beta <- function(...) coef(lm(...))[2]  
  
bsw <- beta( wri ~ rm )  
  
wbsw <- beta( wri ~ rm, w=exp(-2*(length(ri):1)/256) )  
      ## note age = reverse-time weights
```